Graph Library: Graph Container Interface

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1 Getting Started

This paper is one of several interrelated papers for a proposed Graph Library for the Standard C++ Library. The Table 1 describes all the related papers.

Paper	Status	Description
P1709	Inactive	Original proposal, now separated into the following papers.
P3126	Active	Overview, describes the big picture of what we are proposing.
P3127	Active	Background and Terminology provides the motivation, theoretical background, and
		terminology used across the other documents.
P3128	Active	Algorithms covers the initial algorithms as well as the ones we'd like to see in the future.
P3129	Active	Views has helpful views for traversing a graph.
P3130	Active	Graph Container Interface is the core interface used for uniformly accessing graph data
		structures by views and algorithms. It is also designed to easily adapt to existing graph data
		structures.
P3131	Active	Graph Containers describes a proposed high-performance compressed_graph container. It
		also discusses how to use containers in the standard library to define a graph, and how to
		adapt existing graph data structures.
P3337	Soon	Compares the performance and usage syntax with other graph libraries.

Table 1: Graph Library Papers

Reading them in order will give the best overall picture. If you're limited on time, you can use the following guide to focus on the papers that are most relevant to your needs.

Reading Guide

- If you're **new to the Graph Library**, we recommend starting with the *Overview* paper (P3126) to understand the focus and scope of our proposals.
- If you want to **understand the theoretical background** that underpins what we're doing, you should read the *Background and Terminology* paper (P3127).
- If you want to **use the algorithms**, you should read the *Algorithms* paper (P3128) and *Graph Containers* paper (P3131).
- If you want to write new algorithms, you should read the Views paper (P3129), Graph Container Interface paper (P3130), and Graph Containers paper (P3131). You'll also want to review existing implementations in the reference library for examples of how to write the algorithms.
- If you want to use your own graph container, you should read the Graph Container Interface paper (P3130) and Graph Containers paper (P3131).
- If you want to see how the library in this proposal stacks up against other graph libraries in performance and usage syntax, you should read the *Comparison* paper (P3337).

2 Revision History

D3130r0

- Split from P1709r5. Added *Getting Started* section.
- Add default implementation for target_id(g,uv) when the graph type matches the pattern random_access_range<forward_range<integral>> or random_access_range<forward_range<tuple<integral ,...>>>; vertex_id_t<G> also defaults to the integral type given.
- Revised concept definitions, adding sourced_targeted_edge and target_edge_range, and replaced summary table with code for clarity. Also assured that all combinations of adjacency list concepts for *basic*, *sourced* and *index* exist.

- Move text for graph data structures created from std containers from Graph Container Interface to Container Implementation paper.
- Identify all concept definitions as "For exposition only" until we have consensus of whether they belong in the standard or not.

D3130r1

- Add num_edges(g) and has_edge(g) functions. Split function table into 3 tables for graph, vertex and edge functions because it was getting too big.
- Removed the Load Graph Data section with it's load functions from P3130 Graph Container Interface because it unnecessarily complicates the interface with constructors for graph data structures. To complement this, constructors have been added for compressed_graph in P3131 Graph Containers.
- Revised partition functions after implementation in compressed_graph to reflect usage, including: renaming partition_count(g) to num_partitions(g) to match other names used, changed partition_id(g,u) to partition_id(g,uid) because vertices may not exist when the function is called, and removing edges(g,u, pid) because it can easily be implemented as a filter using ranges functionality when target vertices can be in different partitions.

D3130r2

- Add the edgelist as an abstract data structure as a peer to the adjacency list. This causes a reorganization
 of this paper and the addition of a new section for the edgelist.
- Remove unnecessary E edge template parameter in concepts.
- Remove type traits is_unordered_edge and is_ordered_edge because their matching concepts, unordered_edge and ordered_edge, don't need them.

3 Naming Conventions

Table 2 shows the naming conventions used throughout the Graph Library documents.

Template		Variable	
Parameter	Type Alias	Names	Description
G			Graph
	<pre>graph_reference_t<g></g></pre>	g	Graph reference
GV		val	Graph Value, value or reference
EL		el	Edge list
V	vertex_t <g></g>		Vertex
	<pre>vertex_reference_t<g></g></pre>	u,v,x,y	Vertex reference. u is the source (or only) vertex. v is the target vertex.
VId	vertex_id_t <g></g>	uid,vid,seed	Vertex id. uid is the source (or only) vertex id. vid is the target vertex id.
VV	vertex_value_t <g></g>	val	Vertex Value, value or reference. This can be either the user-defined value on a vertex, or a value returned by a function object (e.g. VVF) that is related to the vertex.
VR	vertex_range_t <g></g>	ur,vr	Vertex Range
VI	vertex_iterator_t <g></g>	ui,vi	Vertex Iterator. ui is the source (or only) vertex.
		first,last	vi is the target vertex.
VVF		vvf	Vertex Value Function: $vvf(u) \rightarrow vertex$ value,
			or $vvf(uid) \rightarrow vertex$ value, depending on re- quirements of the consume algorithm or view.
VProj		vproj	<pre>Vertex descriptor projection function: vproj(x) → vertex_descriptor<vid,vv> .</vid,vv></pre>
	partition_id_t <g></g>	 pid	Partition id.
	·	P	Number of partitions.
PVR	<pre>partition_vertex_range_t<g></g></pre>	pur,pvr	Partition vertex range.
E	edge_t <g></g>		Edge
	edge_reference_t <g></g>	uv,vw	Edge reference. uv is an edge from vertices u to v . vw is an edge from vertices v to w .
EId	edge_id_t <g></g>	eid,uvid	Edge id, a pair of vertex_ids.
EV	edge_value_t <g></g>	val	Edge Value, value or reference. This can be either the user-defined value on an edge, or a
			value returned by a function object (e.g. EVF) that is related to the edge.
ER	<pre>vertex_edge_range_t<g></g></pre>		Edge Range for edges of a vertex
EI	vertex_edge_iterator_t <g></g>	uvi,vwi	Edge Iterator for an edge of a vertex. uvi is
			an iterator for an edge from vertices $\tt u $ to $\tt v$.
			$v \mathtt{w} \mathtt{i}$ is an iterator for an edge from vertices \mathtt{v} to \mathtt{w} .
EVF		evf	Edge Value Function: $evf(uv) \rightarrow edge$ value, or $evf(eid) \rightarrow edge$ value, depending on the requirements of the consuming algorithm or view.
EProj		eproj	Edge descriptor projection function: $eproj(x) \rightarrow edge_descriptor$.

Table 2: Naming Conventions for Types and Variables

4 Graph Container Interface

The Graph Container Interface (GCI) defines the primitive concepts, traits, types and functions used to define and access an adacency lists (aka graph) and edgelists, no matter their internal design and organization. For instance, an adjacency list can be a vector of lists from standard containers, CSR-based graph and adjacency matrix. Likewise, an edgelist can be a range of edges from a standard container or externally defined edge types, provided they have a source_id, target_id and optional edge_value.

If there is a desire to use the algorithms against externally defined data structures, the GCI exposes is functions as customization points to be overridden as needed. Likewise, externally defined algorithms can be used to operate on other data structures that meet the GCI requirements. This achieves the same goals as the STL, where algorithms can be used on any container that meets the requirements of the algorithm.

The GCI is designed to support a wider scope of graph containers than required by the views and algorithms in this proposal. This enables for future growth of the graph data model (e.g. incoming edges on a vertex), or as a framework for graph implementations outside of the standard. For instance, existing implementations may have requirements that cause them to define features with looser constraints, such as sparse vertex_ids, non-integral vertex_ids, or storing vertices in associative bi-directional containers (e.g. std::map or std::unordered_map).

Such features require specialized implementations for views and algorithms. The performance for such algorithms will be sub-optimal, but may be preferrable to run them on the existing container rather than loading the graph into a high-performance graph container and then running the algorithm on it, where the loading time can far outweigh the time to run the sub-optimal algorithm. To achieve this, care has been taken to make sure that the use of concepts chosen is appropriate for algorithm, view and container.

All algorithms in this and related proposals require that adjacency list vertices are stored in random access containers and that vertex_id_t<G> is integral. Future designs may relax these requirements, but for now they are required.

5 Adjacency List Interface

5.1 Concepts

This section describes the concepts to describe the adjacency lists used for graphs in the Graph Library. There are a number of qualifiers that are used in concept names.

- **basic** where there is only a vertex id but no vertex reference.
- index where the vertex range is random-access and the vertex id is integral.
- **sourced** where an edge has a source id.

While we belive the use of concepts is appropriate for graphs as a range-of-ranges, we are marking them as "For exposition only" until we have consensus of whether they belong in the standard or not.

5.1.1 Edge Concepts

The types of edges that can occur in a graph are described with the edges concepts. The E edge template parameter allows for different types of edges, such as incoming and outgoing edge types.

```
// For exposition only
template <class G>
concept basic_targeted_edge = requires(G&& g, edge_reference_t<G> uv) { target_id(g, uv); };
template <class G>
concept basic_sourced_edge = requires(G&& g, edge_reference_t<G> uv) { source_id(g, uv); };
template <class G>
concept basic_sourced_targeted_edge = basic_targeted_edge<G> && //
```

```
basic_sourced_edge<G> && //
requires(G&& g, edge_reference_t<G> uv) { edge_id(g, uv); };
template <class G>
concept targeted_edge = basic_targeted_edge<G> && //
requires(G&& g, edge_reference_t<G> uv) { target(g, uv); };
template <class G>
concept sourced_edge = basic_sourced_edge<G> && //
requires(G&& g, edge_reference_t<G> uv) { source(g, uv); };
template <class G>
concept sourced_targeted_edge = targeted_edge<G> && //
sourced_edge<G> && //
requires(G&& g, edge_reference_t<G> uv) { edge_id(g, uv); };
```

There are two edge range concepts.

 $[PHIL: edges(g,u) isn't being used anywhere. We could use basic_adjacency_list in the View and algorithm definitions.]$

5.1.2 Vertex Concepts

The vertex_range concept is the general definition used for adjacency lists while index_vertex_range is used for high performance graphs where vertices typically stored in a vector.

5.1.3 Adjacency List Concepts

The basic adjacency lists add concepts where there is no vertex object, only a vertex id.

```
// For exposition only
template <class G>
concept basic_adjacency_list = vertex_range<G> && //
                            basic_targeted_edge_range<G> && //
                            targeted_edge<G>;
template <class G>
concept basic_index_adjacency_list = index_vertex_range<G> && //
                                 basic_targeted_edge_range<G> && //
                                 basic_targeted_edge<G>;
template <class G>
concept basic_sourced_adjacency_list = vertex_range<G> && //
                                   basic_targeted_edge_range<G> && //
                                   basic_sourced_targeted_edge<G>;
template <class G>
concept basic_sourced_index_adjacency_list = index_vertex_range<G> && //
                                         basic_targeted_edge_range<G> && //
                                         basic_sourced_targeted_edge<G>;
```

The adjacency list concepts bring together the vertex and edge concepts used for core graph concepts. All algorithms initially proposed for the Graph Library use the index_adjacency_list.

```
// For exposition only
template <class G>
concept adjacency_list = vertex_range<G> && //
                      targeted_edge_range<G> && //
                       targeted_edge<G>;
template <class G>
concept index_adjacency_list = index_vertex_range<G> && //
                            targeted_edge_range<G> && //
                            targeted_edge<G>;
template <class G>
concept sourced_adjacency_list = vertex_range<G> && //
                              targeted_edge_range<G> && //
                              sourced_targeted_edge<G>;
template <class G>
concept sourced_index_adjacency_list = index_vertex_range<G> && //
                                   targeted_edge_range<G> &&
                                   sourced_targeted_edge<G>;
```

5.2 Traits

Table 3 summarizes the type traits in the Graph Container Interface, allowing views and algorithms to query the graph's characteristics.

5.3 Types

Table 4 summarizes the type aliases in the Graph Container Interface. These are the types used to define the objects in a graph container, no matter its internal design and organization. Thus, it is designed to be able to reflect all forms of adjacency graphs including a vector of lists, compressed_graph and adjacency matrix.

Trait	Type	Comment
has_degree <g></g>	concept	Is the degree(g,u) function available?
has_find_vertex <g></g>	concept	Are the find_vertex(g,_) functions available?
has_find_vertex_edge <g></g>	concept	Are the <pre>find_vertex_edge(g,_)</pre> functions available?
has_contains_edge <g></g>	concept	Is the contains_edge(g,uid,vid) function available?
<pre>define_unordered_edge<g> : false_type</g></pre>	struct	Specialize to derive from true_type for a graph with unordered edges
unordered_edge <g></g>	$\operatorname{concept}$	
ordered_edge <g></g>	concept	
<pre>define_adjacency_matrix<g> : false_type</g></pre>	struct	Specialize for graph implementation to derive from true_type for edges stored as a square 2-dimensional array
is_adjacency_matrix <g></g>	struct	
is_adjacency_matrix_v <g></g>	type alias	
adjacency_matrix <g></g>	concept	

 Table 3: Graph Container Interface Type Traits

The type aliases are defined by either a function specialization for the underlying graph container, or a refinement of one of those types (e.g. an iterator of a range). Table 5 describes the functions in more detail.

graph_value(g), vertex_value(g,u) and edge_value(g,uv) can be optionally implemented, depending on whether the graph container supports values on the graph, vertex and edge types.

Type Alias	Definition	Comment
graph_reference_t <g></g>	add_lvalue_reference <g></g>	
graph_value_t <g></g>	<pre>decltype(graph_value(g))</pre>	optional
vertex_range_t <g></g>	<pre>decltype(vertices(g))</pre>	
<pre>vertex_iterator_t<g></g></pre>	<pre>iterator_t<vertex_range_t<g>></vertex_range_t<g></pre>	
vertex_t <g></g>	<pre>range_value_t<vertex_range_t<g>></vertex_range_t<g></pre>	
<pre>vertex_reference_t<g></g></pre>	<pre>range_reference_t<vertex_range_t<g>></vertex_range_t<g></pre>	
vertex_id_t <g></g>	<pre>decltype(vertex_id(g,ui))</pre>	
vertex_value_t <g></g>	<pre>decltype(vertex_value(g,u))</pre>	optional
<pre>vertex_edge_range_t<g></g></pre>	<pre>decltype(edges(g,u))</pre>	
<pre>vertex_edge_iterator_t<g></g></pre>	<pre>iterator_t<vertex_edge_range_t<g>></vertex_edge_range_t<g></pre>	
edge_t <g></g>	<pre>range_value_t<vertex_edge_range_t<g>></vertex_edge_range_t<g></pre>	
edge_reference_t <g></g>	<pre>range_reference_t<vertex_edge_range_t<g>></vertex_edge_range_t<g></pre>	
edge_value_t <g></g>	<pre>decltype(edge_value(g,uv))</pre>	optional
The following is only available	ble when the optional source_id(g,uv) is defined for	the edge
edge_id_t <g></g>	<pre>edge_descriptor<vertex_id_t<g>,true,void,void></vertex_id_t<g></pre>	
partition_id_t <g></g>	<pre>decltype(partition_id(g,uid))</pre>	optional
<pre>partition_vertex_range_t<g></g></pre>	vertices(g,pid)	optional

Table 4: Graph Container Interface Type Aliases

There is no contiguous requirement for vertex_id from one partition to the next, though in practice they will often be assigned contiguously. Gaps in vertex_id s between partitions should be allowed.

5.4 Classes and Structs

The graph_error exception class is available, inherited from runtime_error. While any function may use it, it is only anticipated to be used by the load functions at this time. No additional functionality is added beyond that provided by runtime_error.

While we belive the use of concepts is appropriate for graphs as a range-of-ranges, we are marking them as "For exposition only" until we have consensus of whether they belong in the standard or not.

5.5 Functions

Tables 5, 6 and 7 summarize the primitive functions in the Graph Container Interface. used to access an adacency graph, no matter its internal design and organization. Thus, it is designed to be able to reflect all forms of adjacency graphs including a vector of lists, CSR-based graph and adjacency matrix.

Function	Return Type	Complexity	Default Implementation
graph_value(g)	graph_value_t <g></g>	constant	n/a, optional
vertices(g)	vertex_range_t <g></g>	constant	g if random_access_range <g> , n/a otherwise</g>
<pre>num_vertices(g)</pre>	integral	constant	<pre>size(vertices(g))</pre>
<pre>num_edges(g)</pre>	integral	$ \mathbf{E} $	<pre>n=0; for(u: vertices(g))n+=distance(edges(g,u)); return n;</pre>
has_edge(g)	bool	$ \mathbf{V} $	<pre>for(u: vertices(g))if !empty(edges(g, u))return true; return false;</pre>
<pre>num_partitions(g)</pre>	integral	constant	1
<pre>vertices(g,pid)</pre>	<pre>partition_vertex_range_t<g></g></pre>	constant	vertices(g)
<pre>num_vertices(g,pid)</pre>	integral	constant	<pre>size(vertices(g))</pre>

Table 5: Graph Functions

The complexity shown above for num_edges(g) and has_edge(g) is for the default implementation. Specific graph implementations may have better characteristics.

The complexity shown above for vertices(g,pid) and num_vertices(g,pid) is for the default implementation. Specific graph implementations may have different characteristics.

Function	Return Type	ComplexityDefault Implementation		
<pre>find_vertex(g,uid)</pre>	<pre>vertex_iterator_t<g></g></pre>	constant	<pre>begin(vertices(g))+ uid</pre>	
			if random_access_range <vertex_range_t<g>></vertex_range_t<g>	
<pre>vertex_id(g,ui)</pre>	vetex_id_t <g></g>	$\operatorname{constant}$	<pre>(size_t)(ui - begin(vertices(g)))</pre>	
			Override to define a different vertex_id_t <g></g>	
			type (e.g. $int32_t$).	
<pre>vertex_value(g,u)</pre>	vertex_value_t <g></g>	$\operatorname{constant}$	n/a, optional	
<pre>vertex_value(g,uid)</pre>	vertex_value_t <g></g>	$\operatorname{constant}$	<pre>vertex_value(g,*find_vertex(g,uid)) ,</pre>	
			optional	
degree(g,u)	integral	$\operatorname{constant}$	<pre>size(edges(g,u)) if</pre>	
			<pre>sized_range<vertex_edge_range_t<g>></vertex_edge_range_t<g></pre>	
<pre>degree(g,uid)</pre>	integral	$\operatorname{constant}$	<pre>size(edges(g,uid)) if</pre>	
			<pre>sized_range<vertex_edge_range_t<g>></vertex_edge_range_t<g></pre>	
edges(g,u)	vertex_edge_range_t <g></g>	$\operatorname{constant}$	u if forward range <vertex_t<g>> , n/a</vertex_t<g>	
			otherwise	
edges(g,uid)	<pre>vertex_edge_range_t<g></g></pre>	$\operatorname{constant}$	<pre>edges(g,*find_vertex(g,uid))</pre>	
<pre>partition_id(g,uid)</pre>	partition_id_t <g></g>	constant	0	

Table 6: Vertex Functions

The default implementation for the degree functions assumes that vertex_edge_range_t<G> is a sized range to

have constant complexity. If the underlying container has a non-linear size(R) function, the degree functions will also be non-linear. This is expected to be an uncommon case.

Function	Return Type	ComplexityDefault Implementation		
<pre>target_id(g,uv)</pre>	<pre>vertex_id_t<g></g></pre>	constant	(see below)	
<pre>target(g,uv)</pre>	vertex_t <g></g>	constant	<pre>*(begin(vertices(g))+ target_id(g, uv)) if random_access_range<vertex_range_t<g>> && integral<target_id(g,uv)></target_id(g,uv)></vertex_range_t<g></pre>	
edge_value(g,uv)	edge_value_t <g></g>	constant	<pre>uv if forward_range<vertex_t<g>> , n/a otherwise, optional</vertex_t<g></pre>	
<pre>find_vertex_edge(g,u,vid)</pre>	<pre>vertex_edge_t<g></g></pre>	linear	<pre>find(edges(g,u), [](uv)target_id(g,uv)== vid;})</pre>	
<pre>find_vertex_edge(g,uid,vid)</pre>	<pre>vertex_edge_t<g></g></pre>	linear	<pre>find_vertex_edge(g,*find_vertex(g,uid),vid)</pre>	
<pre>contains_edge(g,uid,vid)</pre>	bool	constant	<pre>uid < size(vertices(g))&& vid < size(vertices(g)) if is_adjacency_matrix_v<g> .</g></pre>	
		linear	<pre>find_vertex_edge(g,uid)!= end(edges(g,uid)) otherwise.</pre>	
The following are on	ly available when the	e optional so	urce_id(g,uv) is defined for the edge	
<pre>source_id(g,uv)</pre>	vertex_id_t <g></g>	constant	n/a, optional	
source(g,uv)	<pre>vertex_t<g></g></pre>	constant	<pre>*(begin(vertices(g))+ source_id(g,uv)) if random_access_range<vertex_range_t<g>> && integral<target_id(g,uv)></target_id(g,uv)></vertex_range_t<g></pre>	
edge_id(g,uv)	edge_id_t <g></g>	constant	<pre>edge_descriptor<vertex_id_t<g>,true,void, void>{source_id(g,uv),target_id(g,uv)}</vertex_id_t<g></pre>	

Table 7: Edge Functions

When the graph matches the pattern random_access_range<forward_range<integral>>> or random_access_range< forward_range<tuple<integral,...>>> , the default implementation for target_id(g,uv) will return the integral . Additionally, if the caller does not override vertex_id(g,ui) , the integral value will define the vertex_id_t<G> type.

Functions that have n/a for their Default Implementation must be defined by the author of a Graph Container implementation.

Value functions (graph_value(g), vertex_value(g,u) and edge_value(g,uv)) can be optionally implemented, depending on whether the graph container supports values on the graph, vertex and edge types. They return a single value and can be scaler, struct, class, union, or tuple. These are abstract types used by the GVF, VVF and EVF function objects to retrieve values used by algorithms. As such it's valid to return the "enclosing" owning class (graph, vertex or edge), or some other embedded value in those objects.

find_vertex(g,uid) is constant complexity because all algorithms in this proposal require that vertex_range_t<G>
is a random access range.

If the concept requirements for the default implementation aren't met by the graph container the function will need to be overridden.

5.6 Determining the vertex_id type

To determine the type for vertex_id_t<G> the following steps are taken, in order, to determine its type.

- 1. Use the type returned by vertex_id(g,ui) when overridden for a graph.
- 2. When the graph matches the pattern random_access_range<forward_range<integral>>> or random_access_range<forward_range<tuple<integral,...>>> , use the integral type specified.
- 3. Use size_t in all other cases.

vertex_id_t<G> is defined by the type returned by vertex_id(g) and it defaults to the difference_type of the underlying container used for vertices (e.g int64_t for 64-bit systems). This is sufficient for all situations. However, there are often space and performance advantages if a smaller type is used, such as int32_t or even int16_t. It is recommended to consider overriding this function for optimal results, assuring that it is also large enough for the number of possible vertices and edges in the application. It will also need to be overridden if the implementation doesn't expose the vertices as a range.

5.7 Unipartite, Bipartite and Multipartite Graph Representation

num_partitions(g) returns the number of partitions, or partiteness, of the graph. It has a range of 1 to n, where 1 identifies a unipartite graph, 2 is a bipartite graph, and a value of 2 or more can be considered a multipartite graph.

If a graph data structure doesn't support partitions then it is unipartite with one partition and partite functions will reflect that. For instance, $num_partitions(g)$ returns a value of 1, and vertices(g,0) (vertices in the first partition) will return a range that includes all vertices in the graph.

A partition identifies a type of a vertex, where the vertex value types are assumed to be uniform in each partition. This creates a dilemma because the existing $vertex_value(g,u)$ returns a single type based template parameter for the vertex value type. Supporting multiple types can be addressed in different ways using C++ features. The key to remember is that the actual value used by algorithms is done by calling a function object that retrieves the value to be used. That function is specific to the graph data structure, using the partition to determine how to get the appropriate value.

- std::variant : The lambda returns the appropriate variant value based on the partition.
- Base class pointer: The lambda can call a member function to return the value based on the partition.
- void*: The lambda can cast the pointer to a concrete type based on the partition, and then return the appropriate value.

edges(g,uid,pid) and edges(g,ui,pid) filter the edges where the target is in the partition pid passed. This isn't needed for bipartite graphs.

6 Edgelist Interface

An edgelist is a range of values where we can get the source_id and target_id, and an optional edge_value. It is similar to edges in an adjacency list or edges in the incidence view, but is a distinct range of values that are separate from the others.

Like the adjacency list, the edgelist has default implementations that use the standard library for simple implmentations out of the box. It's also able to easily adapt to externally defined edge types by overriding the <code>source_id(e)</code>, <code>target_id(e)</code> and <code>edge_value(e)</code> functions.

6.1 Namespace

The concepts and types for the edgelist are defined in the std::graph::edgelist namespace to avoid conflicts with the adjacency list.

 $[P_{\rm HIL}$: It would be nice to include them in std::graph, but I'm having difficulting figuring out how to do that based on adjlist and edgelist concepts.]

6.2 Concepts

The concepts for edgelists follow the same naming conventions as the adjacency lists. Non-basic concepts are excluded because there's little reason to include an edge reference for such a simple case.

```
template <class EL> // For exposition only
concept basic_sourced_edgelist = ranges::input_range<EL> &&
                              !ranges::range<ranges::range_value_t<EL>> &&
                              requires(ranges::range_value_t<EL> e) {
                               { source id(e) };
                                { target_id(e) } -> same_as<decltype(source_id(e))>;
                              };
template <class EL> // For exposition only
concept basic_sourced_index_edgelist = basic_sourced_edgelist<EL> &&
                                   requires(ranges::range_value_t<EL> e) {
                                     { source_id(e) } -> integral;
                                     { target_id(e) } -> integral; // redundant, for clarity
                                   };
template <class EL> // For exposition only
concept has_edge_value = basic_sourced_edgelist<EL> && //
                      requires(ranges::range_value_t<EL> e) {
                        { edge_value(e) };
                      };
```

6.3 Traits

Table 8 summarizes the type traits in the Edgelist Interface, allowing views and algorithms to query the graph's characteristics.

Trait	Type	Comment
<pre>is_directed<el> : false_type</el></pre>	struct	When specialized for an edgelist to derive
is_directed_v <el></el>		from true_type , it may be used during graph construction to add a second edge with source_id and target_id reversed.

Table 8: Graph Container Interface Type Traits

6.4 Types

Table 9 summarizes the type aliases in the Edgelist Interface.

The type aliases are defined by either a function specialization for the edgelist implementation, or a refinement of one of those types (e.g. an iterator of a range). Table 10 describes the functions in more detail.

edge_value(g,uv) can be optionally implemented, depending on whether or not the edgelist has values on the edge types.

6.5 Functions

Table 10 shows the functions available in the Edgelist Interface. Unlike the adjacency list, source_id(e) and edge_id(e) are always available.

6.6 Determining the source_id, target_id and edge_value types

Special patterns are recognized for edges based on the tuple and edge_descriptor types. When they are used the source_id(e), target_id(e) and edge_value functions will be defined automatically.

The tuple patterns are

- tuple<integral, integral> for source_id(e) and target_id(e) respectively.

Type Alias	Definition	Comment
edge_range_t <el></el>	EL	
edge_iterator_t <el></el>	<pre>iterator_t<edge_range_t<el>></edge_range_t<el></pre>	
edge_t <el></el>	<pre>range_value_t<edge_range_t<el>></edge_range_t<el></pre>	
edge_reference_t <el></el>	<pre>range_reference_t<edge_range_t<el>></edge_range_t<el></pre>	
edge_value_t <el></el>	<pre>decltype(edge_value(e))</pre>	optional
edge_id_t <el></el>	<pre>edge_descriptor<vertex_id_t<el>,true,void,void></vertex_id_t<el></pre>	
vertex_id_t <el></el>	<pre>decltype(target_id(e))</pre>	

Table 9: Edgelist Interface Type Aliases

Function	Return Type	Complex	ComplexityDefault Implementation		
target_id(e)	<pre>vertex_id_t<el></el></pre>	constant	(see below)		
source_id(e)	<pre>vertex_id_t<el></el></pre>	$\operatorname{constant}$	(see below)		
edge_id(e)	edge_id_t <el></el>	constant	<pre>edge_descriptor<vertex_id_t<el>,true,void, void>{source_id(e),target_id(e)}</vertex_id_t<el></pre>		
edge_value(e)	edge_value_t <el></el>	$\operatorname{constant}$	optional, see below		
contains_edge(el,uid,vid)	bool	linear	<pre>find_if(el, [](edge_reference_t<el> e){ return source_id(e)==uid && target_id(e)== vid})</el></pre>		
<pre>num_edges(el)</pre>	integral	$\operatorname{constant}$	size(el)		
has_edge(el)	bool	$\operatorname{constant}$	<pre>num_edges(el)>0</pre>		

Table 10: Edgelist Interface Functions

- tuple<integral,integral,scalar> for source_id(e), target_id(e) and edge_value(e) respectively.

The edge_descriptor patterns are

- -- edge_descriptor<integral,true,void,void> with source_id(e) and target_id(e) .
- edge_descriptor<integral,true,void,scaler> with source_id(e) , target_id(e) and edge_value(e) .

In all other cases the functions will need to be overridden for the edge type.

7 Using Existing Data Structures

Reasonable defaults have been defined for the adjacency list and edgelist functions to minimize the amount of work needed to adapt existing data structures to be used by the views and algorithms.

Useful defaults have been created using types and containers in the standard library, with the ability to override them for external data structures. This is described in more detail in the paper for Graph Library Containers.

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